A Generalized Poor-Verdú Error Bound for Multihypothesis Testing

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Abstract—A lower bound on the minimum error probability for multihypothesis testing is established. The bound, which is expressed in terms of the cumulative distribution function of the tilted posterior hypothesis distribution given the observation with tilting parameter \( \theta \geq 1 \), generalizes an earlier bound due to Poor and Verdú (1995). A sufficient condition is established under which the new bound (minus a multiplicative factor) provides the exact error probability asymptotically in \( \theta \). Examples illustrating the new bound are also provided.

Index Terms—Channel reliability function, converse channel coding theorems, hypothesis testing, maximum-a-posteriori estimation, probability of error.

I. INTRODUCTION

In [3], Poor and Verdú establish a lower bound to the minimum error probability of multihypothesis testing. Specifically, given two random variables \( X \) and \( Y \) with joint distribution \( P_{X,Y} \), where \( X \) takes values in a finite or countably-infinite alphabet \( \mathcal{X} \) and \( Y \) takes values in an arbitrary alphabet \( \mathcal{Y} \), they show that the optimal maximum-a-posteriori (MAP) estimation of \( X \) given \( Y \) results in the following lower bound on the probability of estimation error \( P_e \):

\[
P_e \geq (1 - \alpha) P_{X,Y} \left\{ (x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}(x \mid y) \leq \alpha \right\} \]

for each \( \alpha \in [0, 1] \), where \( P_{X,Y} \) denotes the posterior distribution of \( X \) given \( Y \) and the prior distribution \( P_X \) is arbitrary (not necessarily uniform). This bound has pertinent information-theoretic applications such as in the proof of the converse part of the channel coding theorem that yield formulas for both capacity and \( \varepsilon \)-capacity for general channels with memory (not necessarily information stable, stationary, etc) [5], [3]. It also improves upon previous lower bounds due to Shannon [4], [3, Eq. (7)] and to Verdú and Han [5], [3, Eq. (9)].

In this work, we generalize the above Poor-Verdú lower bound in (1) for the minimum error probability of multihypothesis testing. The new bound is expressed in terms of the cdf of the tilted posterior distribution of \( X \) given \( Y \) with tilting parameter \( \theta \geq 1 \), and it reduces to (1) when \( \theta = 1 \); see Theorem 1. We also provide a sufficient condition under which our generalized Poor-Verdú bound, without the multiplicative factor \( (1 - \alpha) \), is exact in the limit of \( \theta \) going to infinity. Specifically, the sufficient condition requires having a unique MAP estimate of \( X \) from \( Y \) almost surely in \( P_Y \), where \( P_Y \) is the distribution of \( Y \); see Theorem 2. We present a few examples to illustrate the results of Theorems 1 and 2. Note that we will use the natural logarithm throughout.

II. MAIN RESULTS

Consider two (correlated) random variables \( X \) and \( Y \), where \( X \) has a discrete (i.e., finite or countably-infinite) alphabet \( \mathcal{X} = \{ x_1, x_2, x_3, \ldots \} \) and \( Y \) takes on values in an arbitrary alphabet \( \mathcal{Y} \). The minimum probability of error \( P_e \) in estimating \( X \) from \( Y \) is given by

\[
P_e \triangleq P_Y[X \neq e(Y)].
\]

where \( e(Y) \) is the MAP estimate defined as

\[
e(Y) = \arg \max_{x \in \mathcal{X}} P_{X|Y}(x \mid Y).
\]

Theorem 1: The above minimum probability of error \( P_e \) in estimating \( X \) from \( Y \) satisfies the following inequality

\[
P_e \geq (1 - \alpha) P_{X,Y} \left\{ (x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}^{(\theta)}(x \mid y) \leq \alpha \right\}
\]

for each \( \alpha \in [0, 1] \) and \( \theta \geq 1 \), where for each \( y \in \mathcal{Y} \),

\[
P_{X|Y}^{(\theta)}(x \mid y) \triangleq \frac{P_X^{(\theta)}(x \mid y)}{\sum_{x' \in \mathcal{X}} P_X^{(\theta)}(x' \mid y)}, \quad x \in \mathcal{X},
\]

is the tilted distribution of \( P_{X|Y}(\cdot \mid y) \) with parameter \( \theta \).

Note: When \( \theta = 1 \), the above bound in (4) reduces to the Poor-Verdú bound in (1).

Proof: Fix \( \theta \geq 1 \). We only provide the proof for \( \alpha < 1 \) since the lower bound trivially holds when \( \alpha = 1 \).

From (2) and (3), the minimum error probability \( P_e \) incurred in testing among the values of \( X \) satisfies

\[
1 - P_e = \int_{\mathcal{Y}} \left( \max_{x \in \mathcal{X}} P_{X|Y}(x \mid y) \right) dP_Y(y) = E \left[ \max_{x \in \mathcal{X}} f_x(Y) \right],
\]

where \( f_x(y) \triangleq P_{X|Y}(x \mid y) \). For a fixed \( y \in \mathcal{Y} \), let \( h_j(y) \) be the \( j \)-th element in the set

\[
\{ f_{x_1}(y), f_{x_2}(y), f_{x_3}(y), \ldots \}
\]

such that its elements are listed in non-increasing order; i.e.,

\[
h_1(y) \geq h_2(y) \geq h_3(y) \geq \ldots
\]
and
\[ \{ h_1(y), h_2(y), h_3(y), \ldots \} = \{ f_{x_1}(y), f_{x_2}(y), f_{x_3}(y), \ldots \}. \]

Then
\[ 1 - P_e = E(h_1(Y)). \tag{6} \]

Furthermore, for each \( h_j(y) \) above, define \( h_j^{(y)}(y) \) such that \( h_j^{(y)}(y) \) be the respective element for \( h_j(y) \) satisfying
\[ h_j^{(y)}(y) - f_{x_j}(y) - P_{X|Y}(x_j|y) \leftrightarrow h_j^{(y)}(y) - P_{X|Y}^{(y)}(x_j|y). \]

Since \( h_1(y) \) is the largest among \( \{ h_i(y) \}_{j=1}^{\infty} \),
\[ h_1^{(y)}(y) = \frac{h_1(y)}{1 + \sum_{j=1}^{\infty} h_j(y)/h_1(y)}. \tag{7} \]

is non-decreasing in \( \theta \) for each \( y \); this implies that
\[ h_1^{(y)}(y) \geq h_1(y) \quad \text{for } \theta \geq 1 \quad \text{and } y \in \mathcal{Y}. \tag{8} \]

For any \( \alpha \in [0, 1] \), we can write
\[
P_{X,Y} \left\{ (x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}^{(y)}(x|y) > \alpha \right\} = \sum_{y \in \mathcal{Y}} P_{X,Y} \left\{ x \in \mathcal{X} : P_{X|Y}^{(y)}(x|y) > \alpha \right\} dP_Y(y)
\]
\[ = \sum_{y \in \mathcal{Y}} \left( \sum_{j=1}^{\infty} h_j(y) \cdot 1 \left( h_j^{(y)}(y) > \alpha \right) \right) dP_Y(y)
\]
\[ \geq \sum_{y \in \mathcal{Y}} h_1(y) \cdot 1 \left( h_1^{(y)}(y) > \alpha \right) dP_Y(y)
\]
\[ \geq \sum_{y \in \mathcal{Y}} h_1(y) \cdot 1 \left( h_1(y) > \alpha \right) dP_Y(y)
\]
\[ = E[h_1(Y) \cdot 1 \left( h_1(Y) > \alpha \right)]. \tag{9} \]

where \( 1[\cdot] \) is the indicator function and the second inequality follows from (7). To complete the proof, we next relate \( E[h_1(Y) \cdot 1 \left( h_1(Y) > \alpha \right)] \) with \( E[h_1(Y)] \), which is exactly \( 1 - P_e \). Invoking \([3, \text{eq. (19)}] \), we have that for any \( \alpha \in [0, 1] \) and any random variable \( U \) with \( P_U(|U| < 1) = 1 \), the following inequality holds with probability one
\[ U \leq \alpha + (1 - \alpha) \cdot U \cdot 1(U > \alpha). \]

Thus
\[ E[U] \leq \alpha + (1 - \alpha)E[U \cdot 1(U > \alpha)]. \]

Applying the above inequality to (8) by setting \( U = h_1(Y) \), we obtain
\[ (1 - \alpha) P_{X,Y} \left\{ (x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}^{(y)}(x|y) > \alpha \right\} \geq E[h_1(Y)] \cdot 1(U > \alpha)
\]
\[ = [1 - P_e] \cdot \alpha - (1 - \alpha) - P_e \]
where the first equality follows from (6).

We next show that if the MAP estimate \( e(Y) \) of \( X \) from \( Y \) is almost surely unique in (3), then the bound of Theorem 1, without the \( (1 - \alpha) \) factor, is tight in the limit of \( \theta \) going to infinity.

**Theorem 2:** Consider two random variables \( X \) and \( Y \), where \( X \) has a finite or countably infinite alphabet \( \mathcal{X} = \{ x_1, x_2, x_3, \ldots \} \) and \( Y \) has an arbitrary alphabet \( \mathcal{Y} \). Assume that
\[ P_{X|Y}(e(y)|x) \leq \max_{x \in \mathcal{X}, y \in \mathcal{Y}} P_{X|Y}(x|y) \tag{10} \]
holds almost surely in \( P_Y \), where \( e(y) \) is the MAP estimate from \( y \) as defined in (3); in other words, the MAP estimate is almost surely unique in \( P_Y \). Then, the error probability in the MAP estimation of \( X \) from \( Y \) satisfies
\[ P_e = \lim_{\theta \to \infty} P_{X,Y} \left\{ (x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}^{(y)}(x|y) \leq \alpha \right\} \tag{11} \]
for each \( \alpha \in (0, 1) \), where the tilted distribution \( P_{X|Y}^{(y)}(\cdot|y) \) is given in (5) for \( y \in \mathcal{Y} \).

**Proof:** It can be easily verified from the definitions of \( h_j(\cdot) \) and \( h_j^{(y)}(\cdot) \) that the following two limits hold for each \( y \in \mathcal{Y} \):
\[ \lim_{\theta \to \infty} h_j^{(y)}(y) = \frac{1}{\ell(y)}, \]

where
\[ \ell(y) \triangleq \max\left\{ j \in \mathbb{N} : h_j(y) = h_1(y) \right\} \tag{12} \]
and \( \mathbb{N} \triangleq \{ 1, 2, 3, \ldots \} \) is the set of positive integers, and
\[ \lim_{\theta \to \infty} h_j(y) \cdot 1 \left( h_j^{(y)}(y) > \alpha \right) - \begin{cases} h_j(y) \cdot 1 \left( \frac{1}{\ell(y)} > \alpha \right) & \text{for } j = 1, \ldots, \ell(y); \\ 0 & \text{for } j > \ell(y). \end{cases} \tag{13} \]

As a result, we obtain that for any \( \alpha \in [0, 1] \),
\[ \lim_{\theta \to \infty} P_{X,Y}(x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}^{(y)}(x|y) > \alpha \]
\[ = \lim_{\theta \to \infty} \sum_{j=1}^{\infty} h_j(y) \cdot 1 \left( h_j^{(y)}(y) > \alpha \right) dP_Y(y)
\]
\[ = \sum_{j=1}^{\infty} h_j(y) \cdot 1 \left( \frac{1}{\ell(y)} > \alpha \right) dP_Y(y), \tag{14} \]

where (13) holds by the dominated convergence theorem since
\[ \sum_{j=1}^{\infty} h_j(y) \cdot 1 \left( h_j^{(y)}(y) > \alpha \right) \leq \sum_{j=1}^{\infty} h_j(y) = 1. \]
Furthermore, (14) holds since the limit (in $\theta$) of
\[ a_{\theta,j} \triangleq h_j(y) \cdot 1 \left( h_j^{(\theta)}(y) > \alpha \right) \]
exists for every $j = 1, 2, \ldots$ by (12), hence implying that
\[ \lim_{\theta \to -\infty} \sum_{j=1}^{\infty} a_{\theta,j} = \sum_{j=1}^{\infty} \lim_{\theta \to -\infty} a_{\theta,j} . \]

Now condition (9) is equivalent to
\[ \Pr[\ell(Y) = 1] \triangleq P_Y \{ y \in Y : \ell(y) = 1 \} = 1; \quad (15) \]
thus,
\[
\lim_{\theta \to -\infty} P_{X,Y} \left\{ (x,y) \in X \times Y : P_{X,Y}^{(\theta)}(x,y) > \alpha \right\} \\
= \int Y h_1(y) \cdot 1 \left( 1 > \alpha \right) dP_Y(y) \\
= 1 - P_e, \quad (16)
\]
where (16) follows from (6). This immediately yields that for $0 < \alpha < 1$,
\[
P_e = 1 - \lim_{\theta \to -\infty} P_{X,Y} \left\{ (x,y) \in X \times Y : P_{X,Y}^{(\theta)}(x,y) > \alpha \right\} \\
= \lim_{\theta \to -\infty} P_{X,Y} \left\{ (x,y) \in X \times Y : P_{X,Y}^{(\theta)}(x,y) \leq \alpha \right\} . \quad (17)
\]

**Observation 1:** We first note that since the bound in (4) holds for every $\theta \geq 1$, it also holds in the limit of $\theta$ going to infinity (the limit exists as shown in the above proof):
\[
P_e \geq (1 - \alpha) \lim_{\theta \to -\infty} P_{X,Y} \left\{ (x,y) \in X \times Y : P_{X,Y}^{(\theta)}(x,y) \leq \alpha \right\} \quad (18)
\]
for any $0 \leq \alpha \leq 1$.

Furthermore, if condition (9) does not hold (or equivalently from (15), if $\Pr[\ell(Y) = 1] < 1$), but there exists an integer $L > 1$ such that $\Pr[\ell(Y) \leq L] = 1$, then using (14), we can write (17) as
\[
P_e \geq (1 - \alpha) \left[ 1 - \int Y h_1(y) \cdot 1 \left( \frac{1}{\ell(Y)} > \alpha \right) dP_Y(y) \right] \\
= (1 - \alpha) \left[ \int Y \left( \sum_{j=1}^{\infty} h_j(y) \cdot 1 \left( \frac{1}{\ell(Y)} > \alpha \right) \right) dP_Y(y) \right] \\
= (1 - \alpha) \left[ \int Y \left( \sum_{j=1}^{\infty} h_j(y) \cdot 1 \left( \frac{1}{\ell(Y)} \leq \alpha \right) \right) dP_Y(y) \right] \\
\quad + \sum_{j=L+1}^{\infty} h_j(y) \cdot 1 \left( \frac{1}{\ell(Y)} \leq \alpha \right) dP_Y(y) ; \quad (a) \]

\[
\lim_{\theta \to -\infty} P_{X,Y} \left\{ (x,y) \in X \times Y : P_{X,Y}^{(\theta)}(x,y) \leq \alpha \right\} = v_1 + v_2 \\
= P_e,
\]
as predicted by Theorem 2, since condition (9) holds (since $\ell(Y) = 1$ almost surely in $\mathcal{Y}$, where $\ell(.)$ is defined in (11)).

We next compute the new bound in (4) for $v_1 = 0.27$, $v_2 = 0.33$ and for different values of $\theta \geq 1$ and plot it in Fig. 1, along with Fano’s original bound (referred to as “Fano” in the figure) given by
\[
P_e \geq \frac{3 - I(X; Y) - \log 2}{\log 2} = 0.568348,
\]
Fig. 1. Lower bounds on the minimum probability of error for Example III-A: bound (4) versus $\alpha$ for $\theta = 1, 20, 100$ and Fano’s original and weakened bounds.

and Fano’s weaker (but commonly used) bound

$$P_e \geq 1 - \frac{I(X; Y) + \log 2}{\log 3} = 0.358587$$

shown in [3, Fig. 2] (referred to as “Weakened Fano” in the figure). The case of $\theta = 1$ corresponds to the original Poor-Verdú bound in (1). As can be seen from the figure, bound (4) for $\theta = 20$ and 100 improves upon (1) and both Fano bounds and approaches the exact probability of error as $\theta$ is increased without bound (e.g., for $\theta = 100$ and $\alpha \downarrow 0$, the bound is quite close to $P_e$). In Fig. 2, bounds (4) and (1), maximized over $\alpha \in [0, 1]$, are plotted versus $\theta$. It is observed that when $\theta \geq 16$, bound (4) improves upon (1).

B. Binary Erasure Channel

Suppose that $X$ and $Y$ are respectively the channel input and output of a BEC with erasure probability $\varepsilon$, where $X = \{0, 1\}$ and $Y = \{0, 1, \varepsilon\}$. Let $P_r|X = 0| = 1 - p$ and $P_r|X = 1| = p$ with $0 < p < 1/2$. Then, the MAP estimate of $X$ from $Y$ is given by

$$e(y) = \begin{cases} y & \text{if } y \in \{0, 1\} \\ 0 & \text{if } y = \varepsilon \end{cases}$$

and the resulting error probability is $P_e = \varepsilon p$.

Calculating bound (4) of Theorem 1 yields

$$(1 - \alpha)P_{X,Y} \left\{ (x, y) \in X \times Y : P_{X \mid Y}(x \mid y) \leq \alpha \right\}$$

$$= \begin{cases} 0 & \text{if } 0 \leq \alpha < \frac{p^\theta}{p^\theta + (1-p)^\theta} \\ \varepsilon P(1 - \alpha) & \text{if } \frac{p^\theta}{p^\theta + (1-p)^\theta} \leq \alpha < \frac{(1-p)^\theta}{p^\theta + (1-p)^\theta} \\ (1 - \alpha) & \text{if } \frac{(1-p)^\theta}{p^\theta + (1-p)^\theta} \leq \alpha < 1. \end{cases}$$

Thus, taking $\theta \uparrow \infty$ and then $\alpha \downarrow 0$ in (18) results in the exact error probability $\varepsilon p$. Note that in this example, the original Poor-Verdú bound (i.e., with $\theta = 1$) also achieves the exact error probability $\varepsilon p$ by choosing $\alpha = 1 - p$; however this maximization of $\alpha = 1 - p$ for the original bound is a function of system’s statistics (here, the input distribution $p$) which is undesirable. On the other hand, the generalized bound (4) can here achieve its peak by systematically taking $\theta \uparrow \infty$ and then letting $\alpha \downarrow 0$.

Furthermore, since in this example, $\ell(y) = 1$ for every $y \in \{0, 1, \varepsilon\}$, we have that (9) holds; hence, by Theorem 2, (10) yields

$$P_e = \lim_{\theta \to \infty} P_{X,Y} \left\{ (x, y) \in X \times Y : P_{X \mid Y}(x \mid y) \leq \alpha \right\}$$

$$= \varepsilon P \text{ for } 0 \leq \alpha < 1,$$

where the last equality follows directly from (18) without the $(1 - \alpha)$ factor.

C. Binary Input Observed in Gaussian Noise

We herein consider an example with a continuous observation alphabet $Y \subset \mathbb{R}$, where $\mathbb{R}$ is the set of real numbers. Specifically, let the observation be given by $Y = X + N$, where $X$ is uniformly distributed over $X = \{-1, +1\}$ and $N$ is a zero-mean Gaussian random variable with variance $\sigma^2$. Assuming that $X$ and $N$ are independent from each other, then for $x \in \{-1, +1\}$ and $y \in \mathbb{R}$

$$P_{X \mid Y}(x \mid y) = \frac{1}{1 + \exp \left( \frac{-2x y}{\sigma^2} \right)},$$

which directly yields a MAP estimate of $X$ from $Y$ given by $e(y) = +1$ if $y > 0$ and $e(y) = -1$ if $y \leq 0$. With a resulting error probability of $P_e = \Phi(-1/\sigma)$, where $\Phi(z) \triangleq \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{z} \exp \left( -\frac{t^2}{2} \right) dt$ is the cdf of the standard (zero-mean unit-variance) Gaussian distribution. Furthermore, since $x \in \{-1, +1\}$, we have

$$P_{X \mid Y}^{(0)}(x \mid y) = \frac{1}{1 + \exp \left( \frac{-2x y}{\sigma^2} \right)},$$
and the generalized Poor-Verdú bound (4) yields

\[
P_e \geq (1 - \alpha) P_{X, Y'} \{ (x, y) \in \mathcal{X} \times \mathcal{Y} : P_{X|Y}(x | y) \leq \alpha \} = (1 - \alpha) \int_{-\infty}^{\infty} \log \left( \frac{1}{2\pi\sigma^2} \right) \exp \left[ -\frac{t^2}{2\sigma^2} \right] dt \]  

\[
= (1 - \alpha) \Phi \left( \frac{\alpha}{2\theta} \right) \log \left( \frac{1}{\alpha} - 1 \right),
\]

Now taking the limits \( \theta \uparrow \infty \) followed by \( \alpha \downarrow 0 \) for the right-hand side term in (20) yields exactly \( \Phi \left( \frac{-\alpha}{2} \right) = P_e \); hence the generalized Poor-Verdú bound (4) is asymptotically tight. The bound is illustrated in Fig. 3 for \( \alpha = 0.429858 \) which gives \( P_e = 0.01 \). It can be seen that for \( \theta = 100 \) and \( \alpha \downarrow 0 \), bound (4) is quite close to \( P_e \). Finally note that (19) directly ascertains that condition (9) of Theorem 2 holds; thus \( P_e \) is given by (10).

**IV. CONCLUDING REMARKS**

We generalized the Poor-Verdú lower bound of (1) for the multihypothesis testing error probability. The new bound, given in (4), involves the tilted posterior distribution of the hypothesis given the observation with tilting parameter \( \theta \) and reduces to the original Poor-Verdú bound when \( \theta = 1 \). We established a sufficient condition under which the bound (without its multiplicative factor) provides the exact error probability when \( \theta \rightarrow \infty \). We also provided some examples to illustrate the tightness of the bound in terms of \( \theta \).

In [3], Poor and Verdú used (1) to show an information-spectrum based upper bound to the reliability function \( h(\mathcal{X}^n) \) – i.e., the optimal channel coding error exponent – for general channels [3, Eq. (14)] and they conjectured that the bound is tight. In [1], this bound was shown not to be tight at low rates for memoryless BECs.

We can similarly apply the new bound (4) to obtain a generalized upper bound on \( h(\mathcal{X}^n) \). Specifically, for a general channel [5], [2] \( \mathcal{W} \triangleq \{ W^n = P_{Y^n | X^n} : X^n \rightarrow Y^n \}_{n=1}^{\infty} \) with input

\[
E^*(R) \leq \sup_{X \in \mathcal{Q}(R)} \liminf_{n \rightarrow \infty} \epsilon(P_{X^n | X}^{\theta}(x, y) \downarrow R),
\]

for every rate \( R > 0 \) and \( \theta \geq 1 \) where

\[
E^*(R) \triangleq -\frac{1}{n} \log P_{X^n, W^n} \{ (x^n, y^n) \in \mathcal{X}^n \times \mathcal{Y}^n : \frac{1}{n} \mathcal{J}_{X^n, W^n}(x^n, y^n) \leq R \},
\]

and

\[
\mathcal{Q}(R) \triangleq \{ X : \text{Each } X^n \text{ in } X \text{ is uniformly distributed}
\text{over its support } S(X^n), \text{ and } R < \liminf_{n \rightarrow \infty} \frac{1}{n} \log |S(X^n)| \}.
\]

Also, in light of (17), the following upper bound holds

\[
E^*(R) \leq \sup_{X \in \mathcal{Q}(R)} \liminf_{n \rightarrow \infty} \epsilon(P_{X^n | X}^{\theta}(x, y) \downarrow R),
\]

for any \( R > 0 \). The bound in (22) is exact for a class of channels that satisfy Theorem 2 (which includes the finite-input memoryless Gaussian channel). However, the determination in closed form of this information-spectral multi-letter characteristic for \( E^*(R) \) remains an open challenging optimization problem.

**REFERENCES**


Po-Ning Chen (S’93–M’95–SM’01) was born in Taipei, Taiwan, in 1963. He received the B.Sc. and M.S. degrees in electrical engineering from the National Tsing-Hua University, Taiwan, in 1985 and 1987, respectively, and the Ph.D. degree in electrical engineering from University of Maryland, College Park, in 1994. From 1985 to 1987, he was with Image Processing Laboratory in National Tsing-Hua University, where he worked on the recognition of Chinese characters. During 1989, he was with Star Tech. Inc., where he focused on the development of finger-print recognition systems. After the reception of Ph.D. degree in 1994, he jointed Wan Ta Technology Inc. as a vice general manager, conducting several projects on Point-of-Sale systems. In 1995, he became a research staff in Advanced Technology Center, Computer and Communication Laboratory, Industrial Technology Research Institute in Taiwan, where he led a project on Java-based Network Managements.
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